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### **Integrating fuzzy quality function deployment and linear goal programming for supplier selection**

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### **1. Introduction**

Supplier Selection (SC) is the process of choosing suppliers based on a number of criteria, compatible with firms' conditions. SC is one of the most important tasks of Supply Chain Management (SCM) in today's competitive world, but SCM success is the most important point to grow and progress among other competitors (Khaleie et al., 2012). The primary objective of each organization is to maximize its interests and minimize its costs. Thus, selection of suitable suppliers plays essential role in the supply chain network of each organization as it demands trading off among cardinal and ordinal preferences of decision makers (DM) through an optimal procedure (Bhattacharya et al., 2010). Supplier selection process is the most significant variable in management of modern supply chain networks as, it helps achieving high quality products and customer satisfaction (González et al., 2004). In this paper, important topics for selection of suppliers in a supply chain are presented. Then, a procedure is proposed to select suppliers for a company in a supply chain. In section 2, we review the related literature. In section 3, combination of Fuzzy Quality Function Deployment (FQFD) and Fuzzy Linear Goal Programming (FLGP) for selection of suppliers will be described. In this section, an example with a data set for a company is used to show usage of the proposed method. Finally, the results are presented in section IV.

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# **2. Materials and methods**

### *2.1. Quality function deployment (QFD)*

As mentioned previously, proposed integrated approach is based on House of Quality (HOQ) of QFD methodology, which is widely used as a strong tool in successful companies all around the world (Akao, 1990). QFD was originally developed and implemented in Japan at the Kobe Shipyards of Mitsubishi Heavy Industries in 1972 (Hauser & Clausing, 1988). It is a widely applied customerdriven design and manufacturing tool to translate customer requirements (WHATs) into appropriate product engineering characteristics (HOWs). QFD advantages include higher customer satisfaction, greater customer focus, shorter lead time, and knowledge preservation (Liu, 2009). A crucial and essential activity when using QFD is constructing HOQ, precisely. This includes determination of weights of customer requirements, relationship matrix between customer requirements and engineering characteristics, and correlation matrix among engineering characteristics (For HOQ modeling approaches, see Fig.1) (Akao, 1990; Chan & Wu, 2005; Fung et al., 2003; Vairaktarakis, 1999).



**Fig. 1.** House of Quaity

$$
Rij = \sum (W_i \times R_{ij}) \qquad i = 1, ..., n \quad , \quad j = 1, ..., m \tag{1}
$$

$$
RI_j^* = RI_j + \sum (TK_j \times RK_j) \qquad k = j \qquad , j = 1, ..., m
$$
 (2)

#### *2.2. Linaer goal programming (LGP)*

A Goal Programming (GP) model is useful to deal with multi-criteria decision-making problems where, the goals cannot be optimized, simultaneously. GP helps decision-makers consider several objectives together to find a set of acceptable solutions and to obtain an optimal compromise. It was originally introduced by Charnes and Cooper (1957), and was further developed by Lee (1972), Ignizio (1985), Tamiz et al. (1998), and Chang (2007) purposed GP to minimize deviations in achievement of goals and their aspiration levels. Sharma et al. (1989) proposed a GP formulation for vendor selection to attain goals pertaining to price, quality and lead-time under demand and budget constraints. Buffa and Jackson (1983) also proposed GP to evaluate vendors by their price, quality and delivery. The structure of multiple-goal model is as follows,

 $min Z = [W_1(d, d^+), W_2(d, d^+), ..., W_k(d, d^+)]$ subject to  $f_i(x) + di - di^+$  $= b_i$ , (3) *x*,  $d_i$ ,  $d_i^+$  and  $d_i^- \times d_i^+ = 0$ ,

where Z is vector of weighted goals, x is vector of decision-making variables,  $d_i$  and  $d_i$ <sup>+</sup> are positive and negative deviations from i-th goal, respectively, and  $W_k$  ( $d_i$ ,  $d_i^+$ ) is a linear function from positive and negative deviations by *W* elements of goals.

# *2.3. Fuzzy logic*

Fuzzy set theory was developed to extract primary possible outcomes from information expressed in vague or imprecise terms (Tamiz, 1998). A fuzzy set is defined by a membership function, used to map an item onto an interval [0, 1] that can be associated with linguistic terms (Lee et al., 2008). A triangular fuzzy number (TFN), a special case of a trapezoidal fuzzy number, is a very popular tool in fuzzy applications. In classic set theory, each element of an *X* belongs to set *A* or not, while in fuzzy set theory, each element belongs to set *A* with a definite level of membership. Fuzzy set *A* in *X* is defined as:

$$
A = \left[ (X, \mu_A(X)) / \mu_A(X) \in [0,1] \right] \tag{4}
$$

Usually, several shapes are considered for fuzzy numbers, such as, triangles or trapezoids. Triangular functions, express proximity to a real number and trapezoidal functions express a fuzzy distance. If  $\tilde{A} = (a_1, b_1, c_1)$  and  $\tilde{B} = (a_2, b_2, c_2)$  are two triangular fuzzy numbers, Algebraic mathematical operations on them are defined as follows,

$$
\tilde{A} + \tilde{B} = (a_1 + a_2, b_1 + b_2, c_1 + c_2) \n\tilde{A} - \tilde{B} = (a_1 - c_2, b_1 - b_2, c_1 - a_2) \n\tilde{A} \times \tilde{B} = (a_1 \times a_2, b_1 \times b_2, c_1 \times c_2) \n\frac{\tilde{A}}{\tilde{B}} = (\frac{a_1}{c_2}, \frac{b_1}{b_2}, \frac{c_1}{a_2})
$$
\n(6)

For instance, let  $U = \{VL; L; M; H; VH\}$  be a linguistic set used to express opinions on a group of attributes (VL = very low :(0, 1, 2), L = low :(2, 3, 4), M = medium :(4, 5, 6), H = high :(6, 7,8), VH  $=$  very high :(8, 9, 10)). The linguistic variables of U, can be quantified using triangular fuzzy numbers as follows (Fig. 2):



**Fig. 2.** Linguistic scale for relative importance

# **3. Case study: Ranking suppliers by FQFD and FLGP**

First, an expert team was formed from 5 higher managers of PETROCHEMICAL Co. plus, the researcher to evaluate and select suppliers. If an organization needs the suppliers, experts indicate key purchases, supply requirements and determine supplier evaluation indices. Then, logistics department indicates potential suppliers. Then, brain storming is formed among experts and these criteria are compared in pairs. Then, weights of supplier selection criteria are calculated by goal programming technique. After identification of potential suppliers, situation of each supplier toward each index is determined by linguistic variables or consensus of experts. Finally, ranks of suppliers are determined by FQFD method. Data is analyzed so that primary data are gathered by questionnaires by the following steps.

### *3.1. Step 1:Qualitative requirements of product (What's)*

A purchased product must have four features:

- 1. Product quality  $(B_1)$ : Compatibility of product in production conditions and product performance
- 2. Production cost  $(B_2)$ : Compatibility with future of product and accessible resources
- 3. Delivery performance  $(B_3)$ : Ability of supplier to consider a predetermined delivery date
- 4. After-sell services (B4)

# *3.2. Step 2: Technical and engineering requirements or recognition of supplier's evaluation criteria (How's)*

Using general criteria in this problem provides comparison of goals for all suppliers. Therefore, after analysis of questionnaires and obtaining 47 criteria, expert team identifies necessary criteria to evaluate and select suppliers in a brainstorming session. These criteria are as follows,

- 1. Flexibility in condition of changing strategy and market  $(C_1)$
- 2. Experience of supplier  $(C_2)$
- 3. Financial stability  $(C_3)$
- 4. Optimum feature  $(C_4)$ : Previous performance of suppliers helps selection of them.
- 5. Quality system licenses  $(C_5)$
- 6. Flexibility in response to customer requests  $(C_6)$
- 7. Geographical location  $(C_7)$

# *3.3. Step 3: Finding relation between customers' needs and technical definitions*

Finding relation between customers' needs and technical definitions is very complex because each technical definition may influence on many customers' needs and vice versa. Views of each employee group about linguistic variables defined based on triangular fuzzy numbers are used to determine communications matrix for quality house. This is determined after brainstorming and is recorded in Table 2. Then, average of employees' views is recorded in the quality house. (Fig.3)

$$
RATING = \{r_{ij}, where \ i = 1, ..., k \ and \ j = 1, ..., m\}
$$
  
\n
$$
r_{ij} = \frac{1}{n} \times (r_{ij1} + \dots + r_{ijn})
$$
\n(9)

where  $k =$  number of the "WHATs",  $m =$  number of the "HOWs" and  $n =$  number of the decisionmakers (in our case,  $k = 4$ ,  $m = 7$  and  $n = 5$ ). This time, the RATING is the matrix of the "how"-"what" correlation scores, whose r<sub>ij</sub> elements represent an aggregate correlation score between the ith "what" and the jth "how". Here again, the r<sub>ij</sub> elements are triangular fuzzy numbers defined by the triplets  $r_{ij} = (r_{ij\alpha}, r_{ij\beta} , r_{ij\gamma})$ .

**Table 2** 





Usually, developmental analysis method is used to rank fuzzy numbers. In some cases, this method has unsuitable results, namely, many low importance factors may obtain zero weight. To remove this problem, GP method is used; this method has not weaknesses of developmental analysis method and has precise and dependable results. This is a linear GP where  $W_L$ ,  $W_M$ ,  $W_U$  and fuzzy weight of pair comparison matrix will be obtained by solving it (Tavakoli et al., 2013).

$$
\min J = \sum_{i=1}^{n} (\varepsilon_{i}^{+} + \varepsilon_{i}^{-} + \gamma_{i}^{+} + \gamma_{i}^{-} + \delta_{i}) = e^{T} (E^{+} + E^{-} + \Gamma^{+} + \Gamma^{-} + \Delta)
$$
\nsubject to:

subject to:



weights of criteria for selection of suppliers are determined by FLGP method and using pair comparison matrix of TABLE 3. Pair comparison matrix is as follows, obtained by consensus of experts.

### **Table 3**

Pair comparison matrix up on triangular fuzzy numbers (Priority of criteria)



Then, adjustment of non-fuzzy matrices for  $A_L$ ,  $A_M$ ,  $A_u$ :



Weights of evaluation criteria for selection of suppliers are obtained by LGP. In consequence, linear GP models based on pair comparison matrix are formed. The results of optimal solutions are summarized in Table 4.

Therefore, as indicated in matrix of relative importance of evaluation and selection criteria of suppliers, product quality  $(C_2)$  has the highest importance and delivery performance  $(C_3)$  has the lowest importance. Applied to a triangular fuzzy number  $Wi = (W_i^L; W_i^M; W_i^U)$  the approach produces a score identified by this value and ranking is shown in Table 4.

$$
W_i = \frac{W_i^l + [(W_i^U - W_i^L) + (W_i^M - W_i^l)]}{3}
$$
\n(11)



Fuzzy weights for evaluation and selection criteria of suppliers



*3.5. Step 5: Development of technical and engineering requirements (prioritizing technical and engineering specifications of product):*

We can now complete the HOQ, calculating the weights of the "HOWs", averaging the aggregate weighted r<sub>ij</sub> correlation scores with the aggregate weights of the "WHATs" W<sub>i</sub>, according to the equation. The above relative and exact rates show cases that must be concentrated. The absolute and relative weights are as follows,

$$
WEIGHT_{SHOW} = \{W_j, Where \ j = 1, ..., m\}
$$
  
\n
$$
W_j = \frac{1}{k} \times [(r_{j1} \times w_1) + \dots + (r_{jk} \times w_k)]
$$
\n(12)

where the usual conventions are assumed for  $k$  and  $m$ . Each  $W_i$  on the WEIGHTS HOW vector represents the weight of each supplier attribute. The *Wj* are, once again, triangular fuzzy numbers defined by means of the triplets  $(W_{i\alpha}, W_{i\beta}, W_{i\gamma})$ . The fuzzy values for the weights of the ''HOWs'' are shown in the Fig. 3.

### *3.6*. *Step 6*: *Development of mutual communications matrix among technical specifications of service product:*

Correlations among supplier assessment criteria (''HOWs'') are contained in the ''roof'' of HOQ (Fig. 3). This step in construction of HOQ enables the team members to keep track of pairs of ''HOWs''. This matrix contains positive and negative correlations between pairs of ''HOWs'' using, the same symbols as Hines et al (1998). The completed fuzzy-HOQ is illustrated below (Fig. 3).



**Fig. 3.** HOQ

*3.7. Ranking Suppliers* 

In this study, 7 suppliers were selected by consensus of experts of PETROCHEMICAL Co. according to maximum purchase rates. This evaluation is shown in Table 5. Therefore, to evaluate and rank suppliers of PETROCHEMICAL Co. we have:

SUPPLIER RATING = {SR<sub>hj</sub>, Where 
$$
h = 1, \ldots, p
$$
,  $j = 1, \ldots, m$ }

\nSR<sub>hj</sub> =  $\frac{1}{n} \times [sr_{hj1} + \cdots + sr_{hjn}]$ 

\nwhere  $\underline{m}$  is the number of attributes ("HOWa"),  $\underline{n}$  is the number of numbers,  $\underline{n}$  is the number of

where, *m* is the number of attributes (''HOWs''), *p* is the number of suppliers, *n* is the number of decision-makers, and *SRhj* is the (fuzzy) evaluation expressed by the n-th decision maker for the h-th supplier regarding to the j-th attribute. The SUPPLIER RATING matrix contains aggregate assessments  $SR<sub>hi</sub>$  of the h-th supplier for the j-th attribute. The elements in this matrix are also triangular fuzzy numbers identified by triplets  $SR<sub>hi</sub> = (SR<sub>hia</sub>; SR<sub>hib</sub>; SR<sub>hig</sub>)$ .

The last step, in this procedure involves calculating the FSI for each supplier; this index expresses the degree to which each supplier satisfies a given requirement. The  $FSI<sub>h</sub>$  index is a triangular fuzzy number obtained from the previously calculated aggregate scores, multiplied by the weights for each assessment criterion. The equation is as follows,

$$
FSI = \{FSI_h, Where \ h = 1, ..., p\}
$$
  
\n
$$
FSI_h = \frac{1}{m} \times [(SR_{h1} \times w_1) + \dots + (SR_{hm} \times w_m)]
$$
\n(14)

where, the previously adopted conventions apply for p and m.

Supplier	C1		C <sub>2</sub>					C <sub>3</sub>					C4					C5				C6					C7							
DM	DM 2	DM $\overline{3}$	DM	DM	DM	DM 2	DM	DM $\overline{4}$	DM -5	DM	DM 2	DM	DM	DM -5	DM	DM 2	DM $\mathcal{F}$	DM $\overline{4}$	DM -5	DM	DM 2	DM	DM	DM -5	DM	DM 2	<b>DM</b> $\mathcal{E}$	DM	DM -5	DM	DM 2	DM.	<b>DM</b>	DM $5^{\circ}$
$1$ H	M	$H$ M		M		VH VH	H	H	VH	VL	L	L.	$\mathbf{M}$	$\mathbf{L}$		H VH	<b>VH</b>	VH	VH	M	M	M	M	M	H	H	<b>VH</b>	H	H	H	H		VH H H	
2 VH	H		H VH H			VH VH VH H				VH L				VL VL L VL M L			L.	L	$\mathbf{L}$	$\mathbf{L}$			VL VL L VL H			H	H	H	H				$L \quad L$	
$3$ M	M	L	M	M	H	H	M	M	H	VH	VH	<b>VH</b>	H	<b>VH</b>	L.				L	M	M	M	M	M			<b>VL</b>			M	M			$M$ $M$
4 H	M	H	M	M	M	M	M	M	M						H	VH	VH	H	VH						VH	VH	VH	H	VH	H	H	H		$H$ H
$5$ H	H	VH H			H VH VH		$\mathbb{E}[\mathbf{V}]\mathbf{H}$ .	$-$ H $-$	VH	M	L	$\mathbf{L}$	M	L H VH VH				<b>VH</b>	VH	$-L$	$-L$		L L L M			VL <b>1</b>	H	H	VL	$-L$		VL VL L VL		
6 H	H	H	H			$H$ $H$ $H$	M	H	H	L.	$\mathbb{L}$	- L -		M L M M M				M M			$L \quad L$		VL L L H			H	H	H	H		VL VL VL		L VL	
7 H	M	H	M	M	<b>VH</b>	VH	H	H	<b>VH</b>	<b>VL</b>			M		H	<b>VH</b>	<b>VH</b>	<b>VH</b>	<b>VH</b>	M	M	M	M	M	H	H	<b>VH</b>	H	H	H	H	<b>VH</b>		H

**Table 5**  Evaluation of the suppliers

The FSI vector contains the FSIh indexes for each supplier, which are triangular fuzzy numbers as usual, defined by the triplets  $FSI_h = (FSI_{ha}; FSI_{hb}; FSI_{hg})$ , the components of which can be calculated as follows:

$$
FSI_{hx} = \frac{1}{m} \sum_{i=1}^{m} SR_{hjx} . W_{j\alpha}
$$
 (15)

$$
FSI_{h\beta} = \frac{1}{m} \sum_{j=1}^{m} SR_{hj\beta} . W_{j\beta}
$$
 (16)

$$
\text{FSI}_{\text{h}\gamma} = \frac{1}{m} \sum_{j=1}^{m} \text{SR}_{\text{hj}\gamma} \cdot W_{j\gamma} \tag{17}
$$

Finally, for this case, the FSIh indexes are given in Table 6:

# **Table 6**

Ranking suppliers



Applied to a triangular fuzzy number  $FN = (FN_{\alpha}, FN_{\beta}, FN_{\nu})$ , the Facchinetti et al. (1998) approach produces a score identified by this value.

$$
\frac{FN_{\alpha} + 2FN_{\beta} + FN_{\gamma}}{4}
$$
 (18)

Using the fuzzy ranking principle, these fuzzy ratings produce the following ranking order for the suppliers:

Sup 1>Sup 7>Sup 4>Sup 3>Sup 5>Sup 2>Sup 6

where, ">" means "better than".

#### **4. Conclusion**

Supplier selection is one of the most important problems in each manufacturing company. In order to increase competitive advantages, companies must have an efficient supplier selection system (Sanayei, et al., 2008). In this paper, an integrated approach for supplier selection has been proposed. The study has explained two different methods, F-QFD and F-LGP, and then, the proposed combined approach were introduced. Alternative suppliers and the set of criteria have been determined according to the views of the decision making team, and the weights for the criteria in F-QDF method were assigned with regards to decision-making team's experiences and conviction. The F-LGP approach endeavored to minimize the overall deviations in the objective function and F-QFD method has been used in order to rank the suppliers. The result in PETROCHEMICAL Co. shows, that this company must use the 7 obtained criteria to evaluate its suppliers, or at least it must prioritize these 7 criteria than the others. The second result is that PETROCHEMICAL Co. must use this priority to rank its suppliers. For example, if these 7 suppliers supply a common product, PETROCHEMICAL Co. must select the supplier with higher rank. The used models in this research are capable for decision-making of managers. However, regarding to the existing limitations in each model, we propose to use these model in combination, because by this method, limitation of a model will be covered by another. The proposals for future researchers are:

- Fulfillment of this research in other organizations and comparing the results
- Study of risk and its calculation in decision-making problems
- Repetition of this research by other new methods
- Briefing the goal of this research and concentration on the limited goals

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